

# Bayesian constraint of a gridcolumn statistical model of total water content with high-resolution satellite cloud observations

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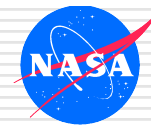
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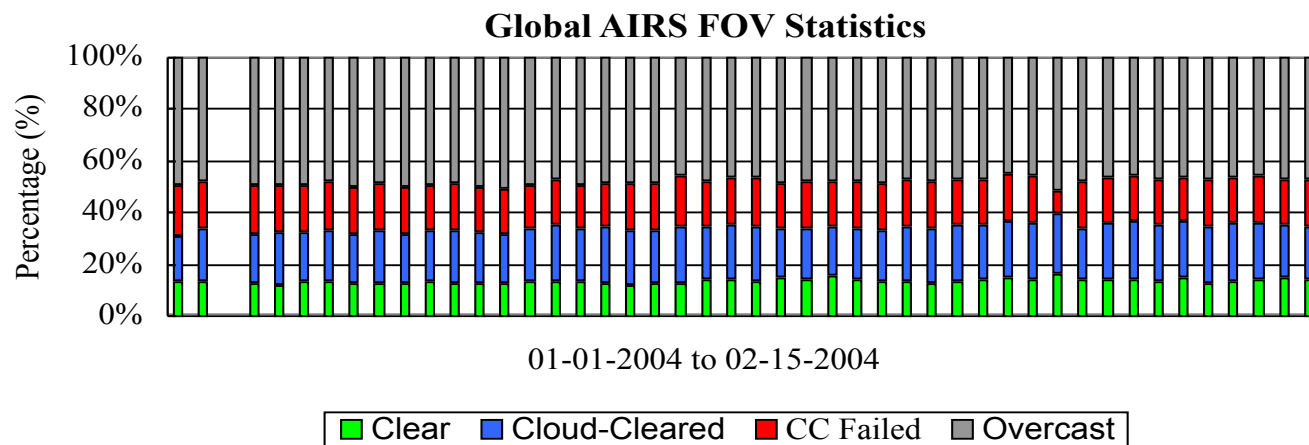
*NASA Sounder Science Team Meeting  
Greenbelt, Maryland, Nov. 13-16, 2012*

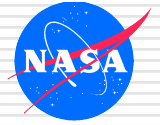


# Motivation

## Limited use of satellite radiances due to clouds

- Direct use of cloudy data is currently hampered by complexity and computational expense of cloudy radiative transfer calculations
- Currently, cloud-affected IR radiances are ignored or parameterized by simple gray-body assumption in most operational DA systems, and cloud-affected solar radiances are not assimilated at all.
- Roughly 13% of considered AIRS FOVs are clear, and another 20% can be cloud-cleared successfully... the rest go unused.





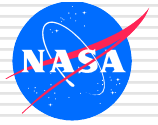
# Standard 3D-Variational Formulation

$$J(\mathbf{x}_k) = \frac{1}{2}(\mathbf{x}_k - \mathbf{x}_k^b)^T \mathbf{B}^{-1}(\mathbf{x}_k - \mathbf{x}_k^b) + J_c \\ + \frac{1}{2}[\mathbf{h}(\mathbf{x}_k) - \mathbf{y}_k]^T \mathbf{R}_k^{-1}[\mathbf{h}(\mathbf{x}_k) - \mathbf{y}_k]$$

where

- ▷  $\mathbf{x}_k$  is the 3d state vector (control variable).
- ▷  $\mathbf{y}_k$  and  $\mathbf{x}_k^b$  are the observation and background state vectors, respectively.
- ▷  $\mathbf{h}_k$  is the nonlinear observation operator.
- ▷  $\mathbf{B}$  and  $\mathbf{R}_k$  are the background and observation error covariances, respectively.

1. Cloud properties are not smooth like temperature and have strong subgrid-scale variability.
2. Cloud observables are not tangent-linear sensitive to *equilibrium* perturbations in the control total water vector for sub-saturated (clear) grid-columns.



# Cloud Data Assimilation

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- ❑ We cannot simply insert clouds in the model
    - We need to convince the model to make clouds.
  - ❑ Data retention requires a high degree of consistency in cloud representation by GCM and assimilation algorithms.
  - ❑ Improved background cloud distributions are essential for effective assimilation of cloudy radiances in 3D/4D Var.
  - ❑ Validation: CloudSat, CERES, SRB.
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Cloud Top Pressure (hPa)



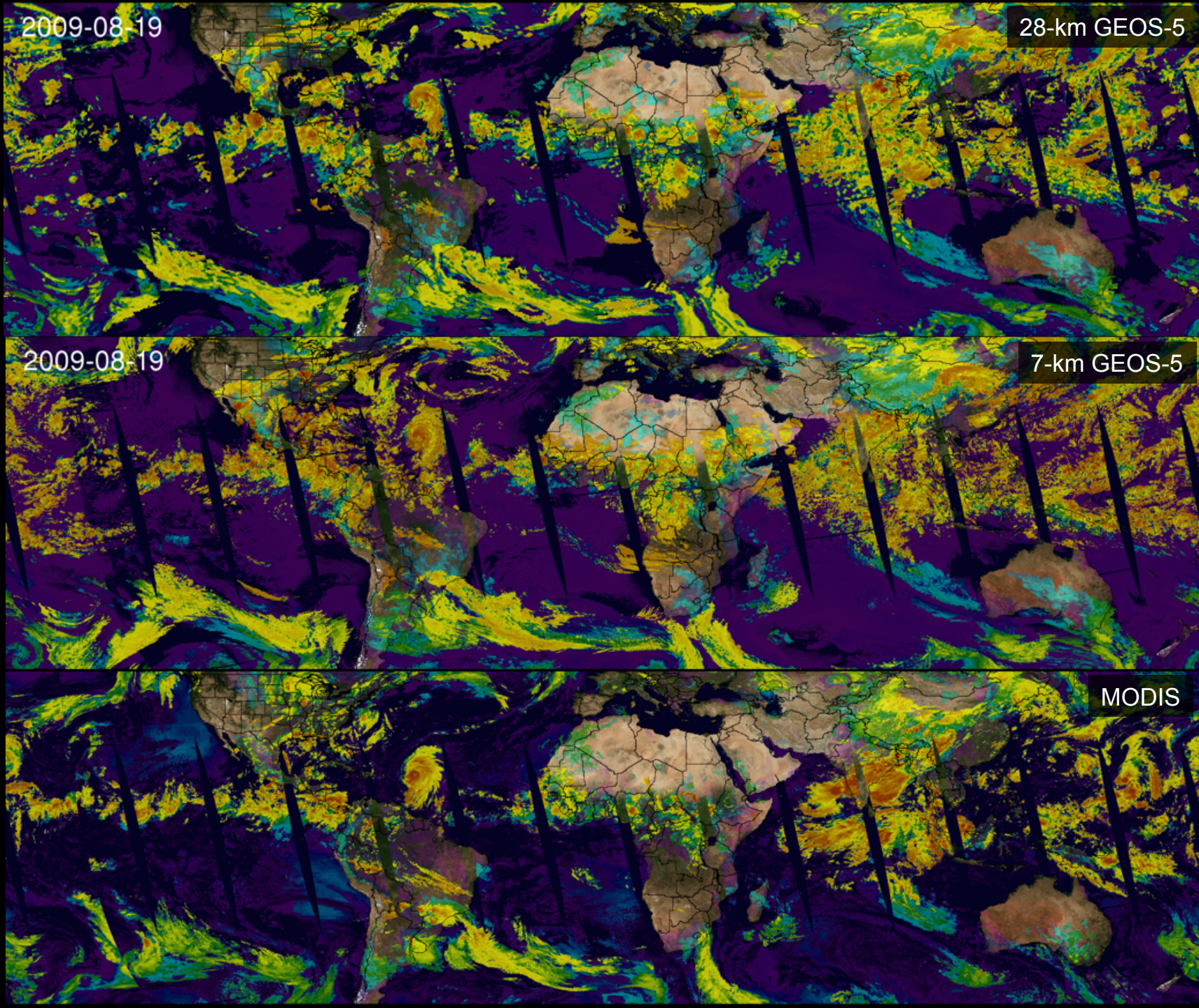
2009-08-19

28-km GEOS-5

2009-08-19

7-km GEOS-5

MODIS





Cloud Optical Thickness



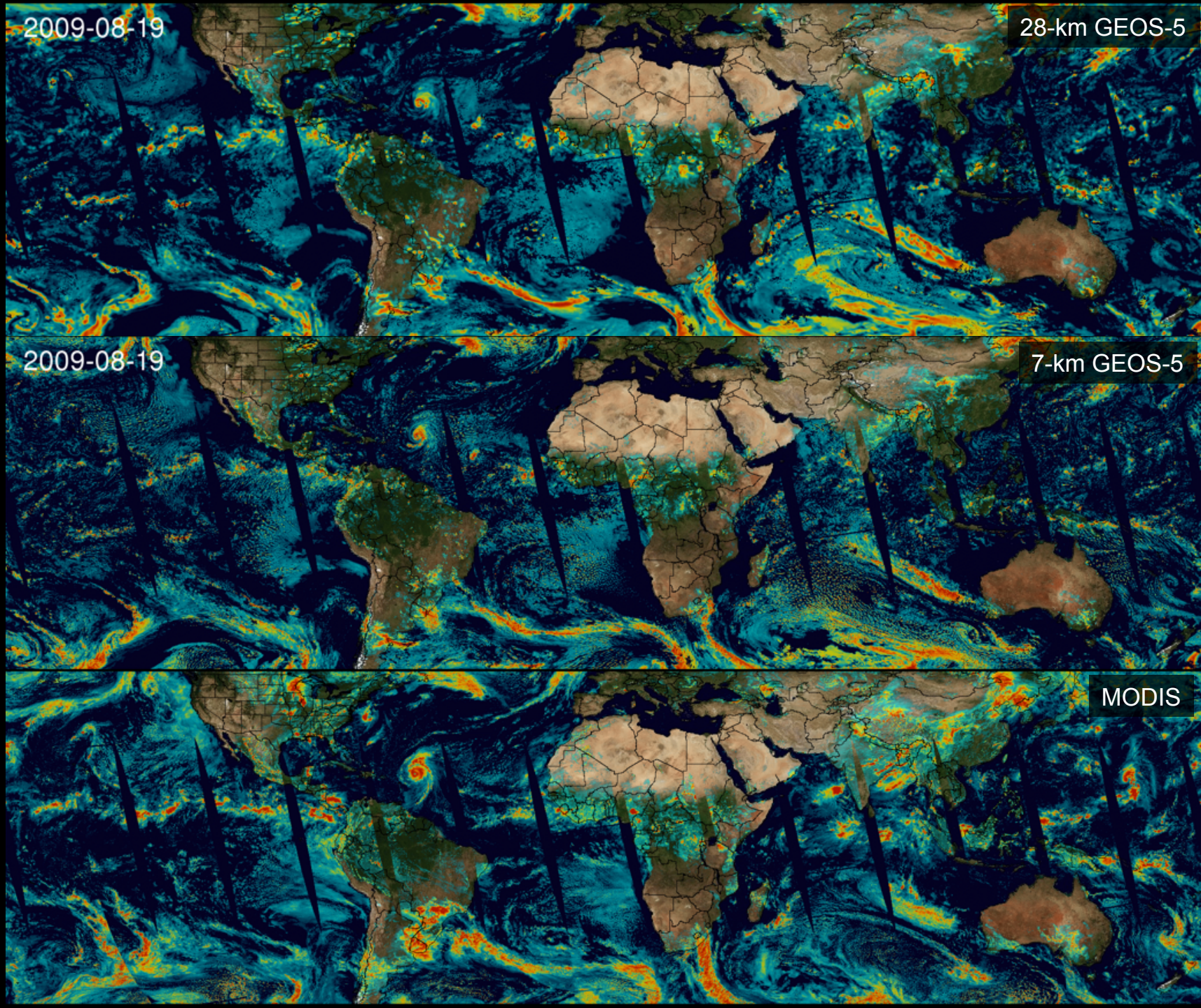
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28-km GEOS-5

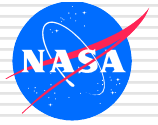
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7-km GEOS-5

MODIS





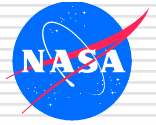


# Statistical Cloud Schemes

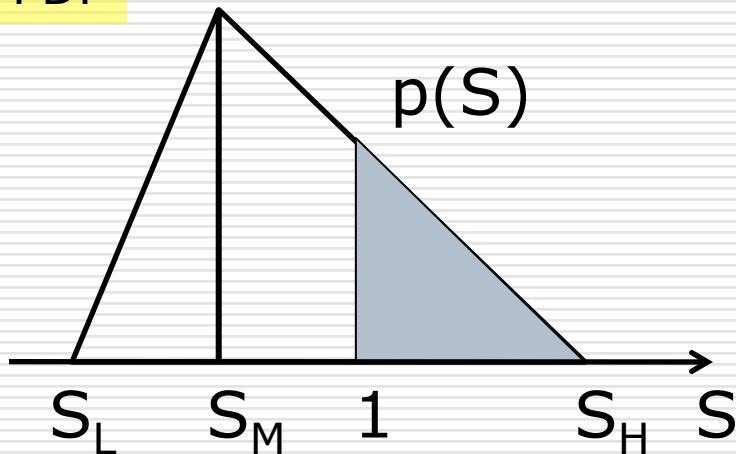
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- ❑ Many recent GCM cloud parameterizations represent sub-gridscale moisture variability using parameterized probability distributions (PDFs) of total water (vapor + condensate).
  - ❑ Our goal is to use high resolution satellite data to constrain a grid-column of such total water PDFs.
  - ❑ Cloud optical depth constrains the column integrals.
  - ❑ IR brightness temperature and cloud top pressure give some information on vertical distribution of moisture in the column.
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# Total Water Triangular PDF Single Gridbox



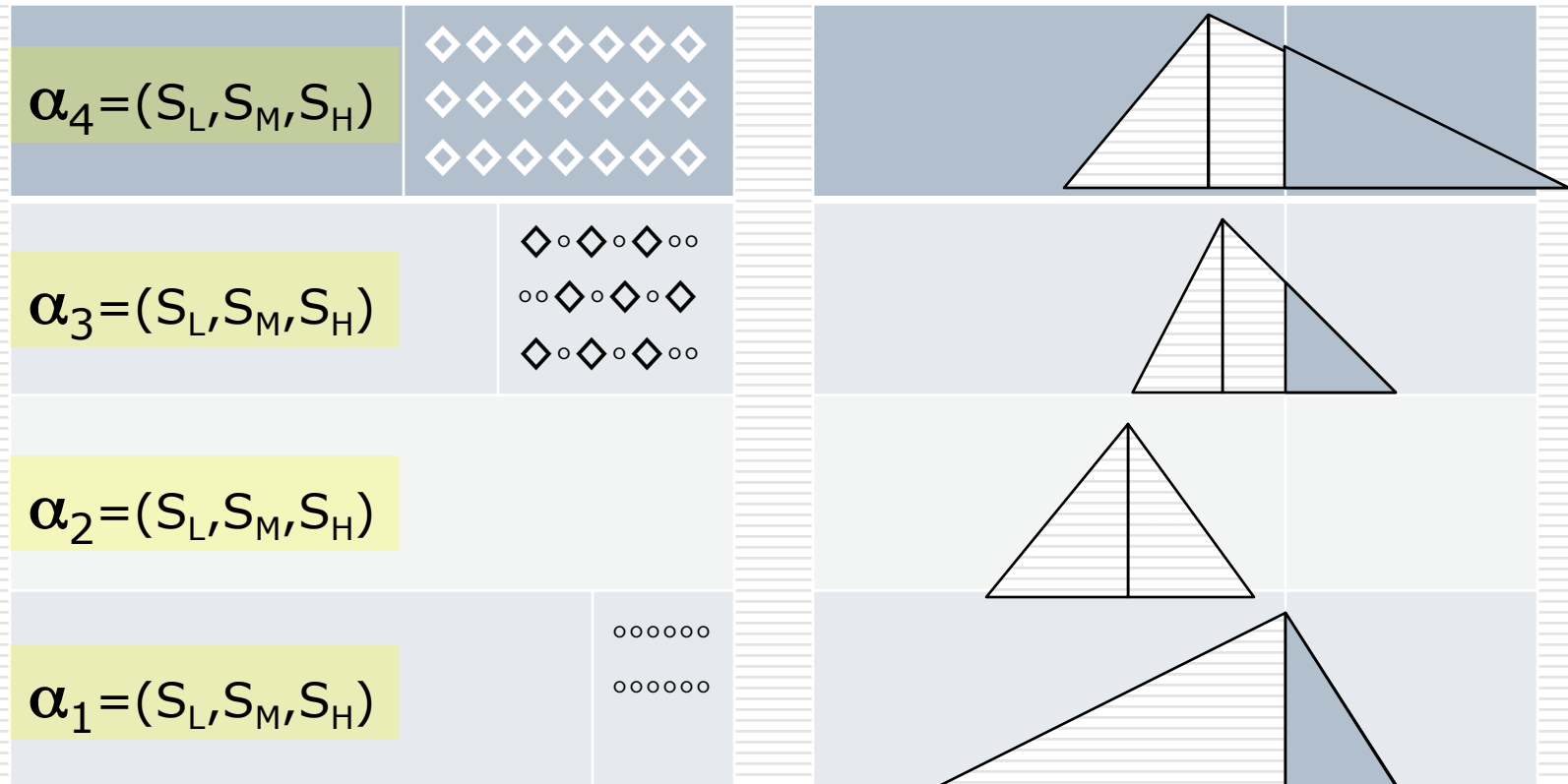
PDF



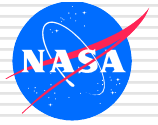
$$S = (q_v + q_L + q_I) / q_S(T)$$
$$p(S) = p(S; \alpha = [S_L, S_M, S_H])$$

- A simple PDF having skewness
- Given  $(S_L, S_M, S_H)$  we can compute
  - $c_F$ , cloud fraction
  - $q_V$ , vapor
  - $q_C = q_L + q_I$
- Conversely, given  $(c_F, q_V, q_C)$  we can reconstruct the PDF

# Grid Column Statistical Model



- Copula used to couple layer PDFs (Norris et al. 2008)



# Multidimensional CDF for a Grid Column

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$$P(S_1, \dots, S_K) = P(S_1, \dots, S_K; \alpha_1, \dots, \alpha_K, \beta)$$

where

- $K$  number of vertical layers
  - $S$  total water variable
  - $\alpha$  PDF parameters for each layer
  - $\beta$  controls vertical coherence of layers
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# Bayesian Parameter Estimation

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- Within a grid column, consider a set of measurements

$$\mathbf{y} = (y_1, \dots, y_P)$$

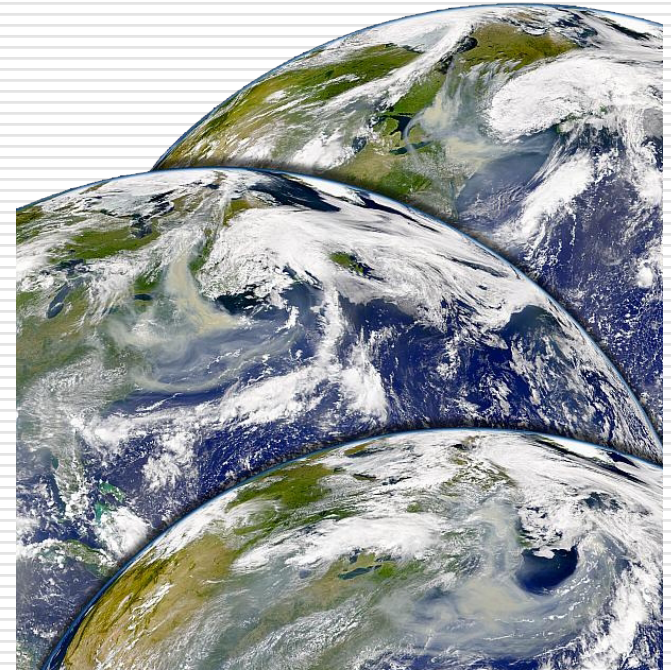
say MODIS cloud top pressure, cloud optical depth

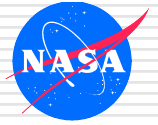
- Goal:
  - estimate PDF parameters  $\alpha_k$
  - Given the observations  $\mathbf{y}$

- Bayes theorem:

$$p(\alpha|\mathbf{y}) \sim p(\mathbf{y}|\alpha) p(\alpha)$$

- Maximum *a posteriori* estimation
  - Find  $\alpha$  that maximizes  $p(\alpha|\mathbf{y})$
  - Can also characterize  $p(\alpha|\mathbf{y})$  form





# Parameter Estimation

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## □ Evaluating $p(\mathbf{y}|\alpha)$

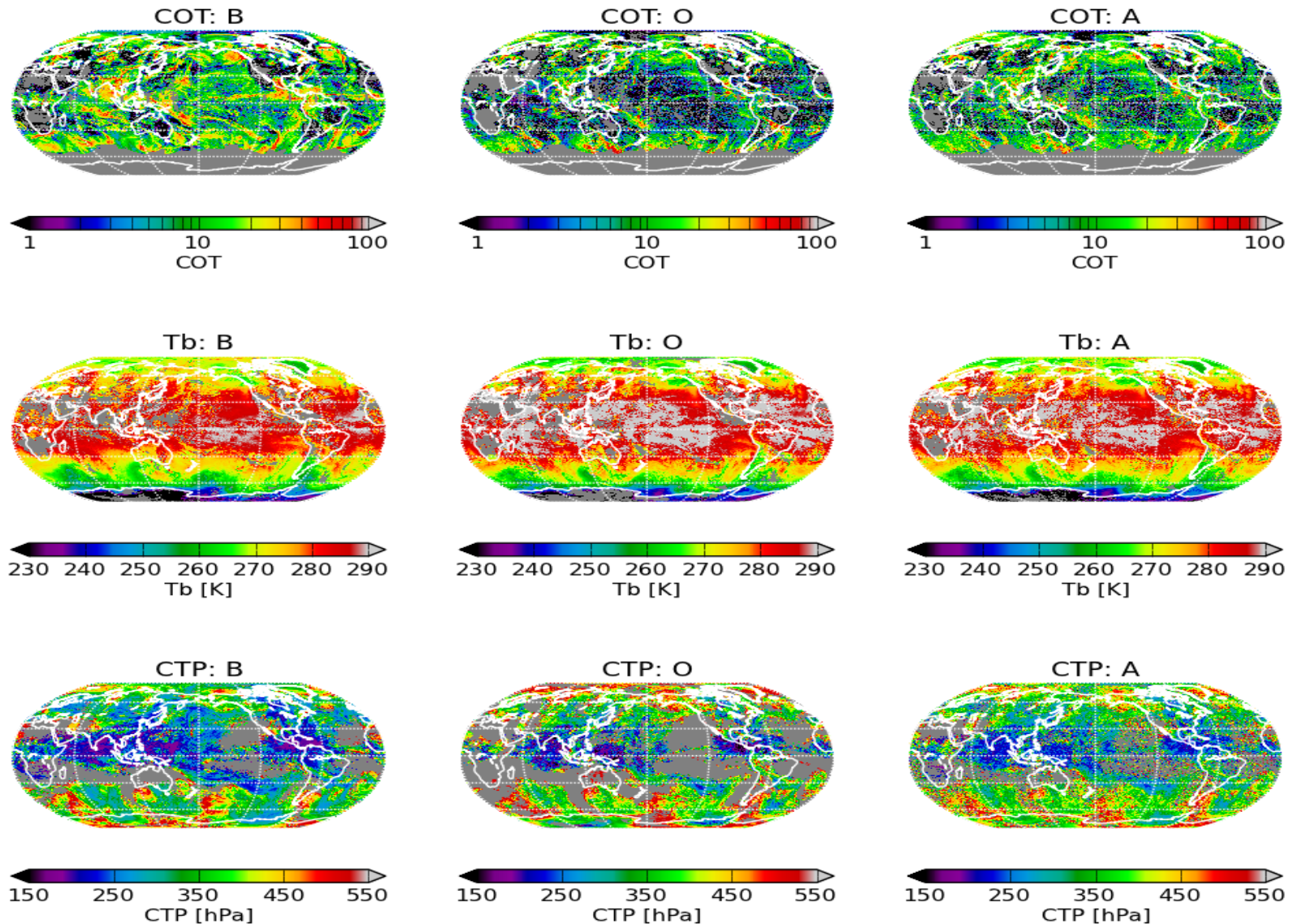
- Given  $\alpha$ , generate sub-columns by sampling the multidimensional grid-column PDF of S
- Simulate observables for each sub-column
- Use these simulated sub-columns to obtain a *Kernel Density Estimate* (KDE) of  $p$  at the observational points  $\mathbf{y}$

## □ Optimization

- Markov Chain Monte Carlo method
    - Modified Metropolis-Hastings algorithm
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# A one day analysis of MODIS Aqua and Terra



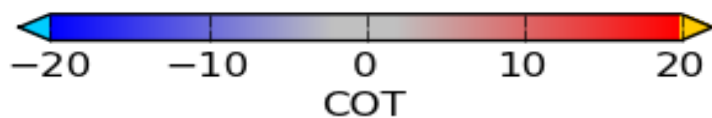
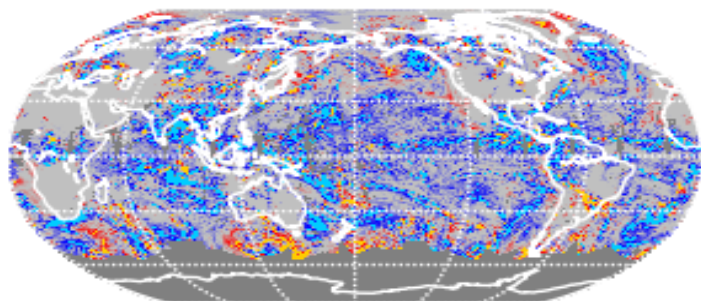
bkg

obs

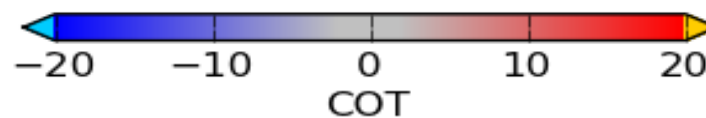
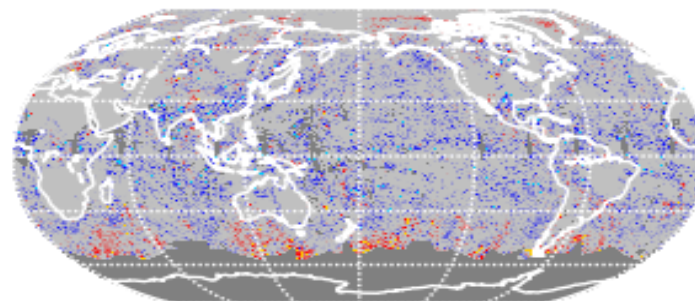
ana

# Reduction in Cloud Property Biases

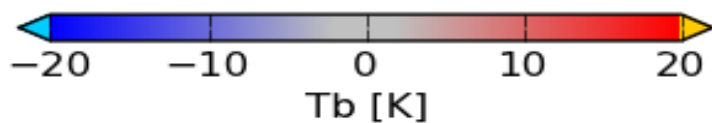
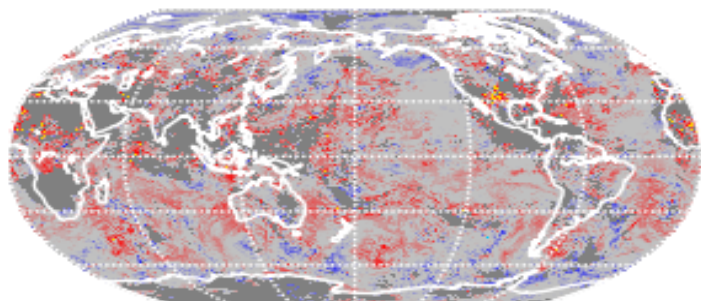
COT: O-B



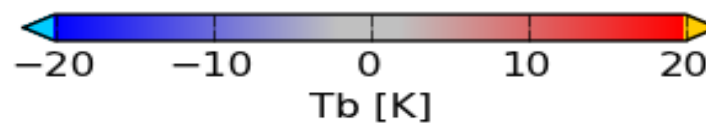
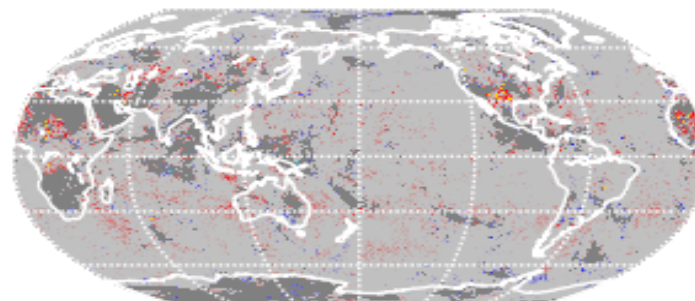
COT: O-A



Tb: O-B

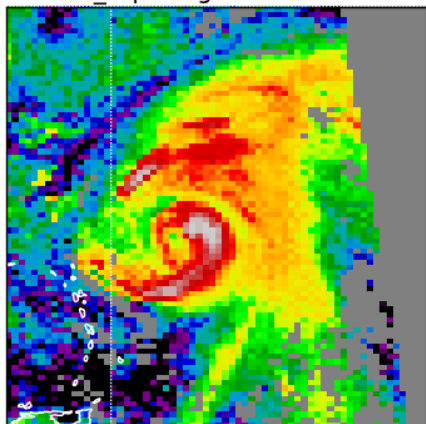


Tb: O-A



# Hurricane Bill

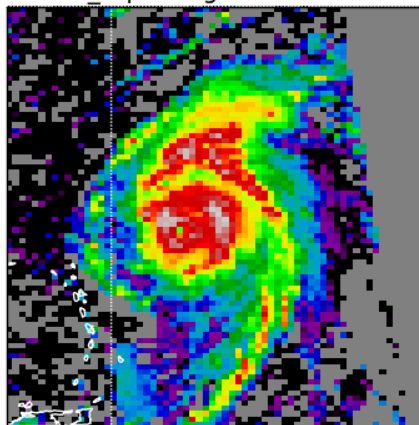
Ks128n128 Aq: IC: gridcolumn mean COT



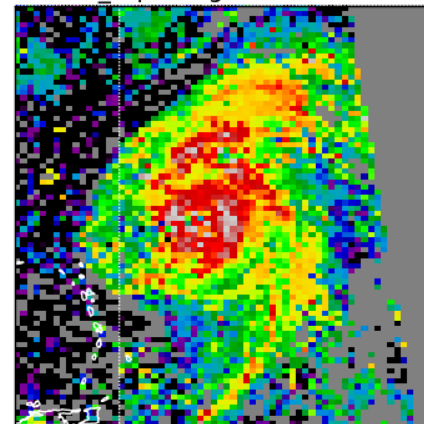
bkg

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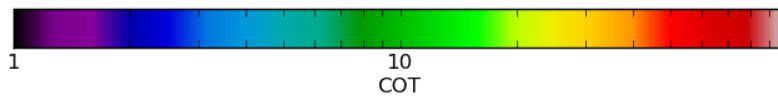
Ks128n128 Aq: OB: gridcolumn mean COT



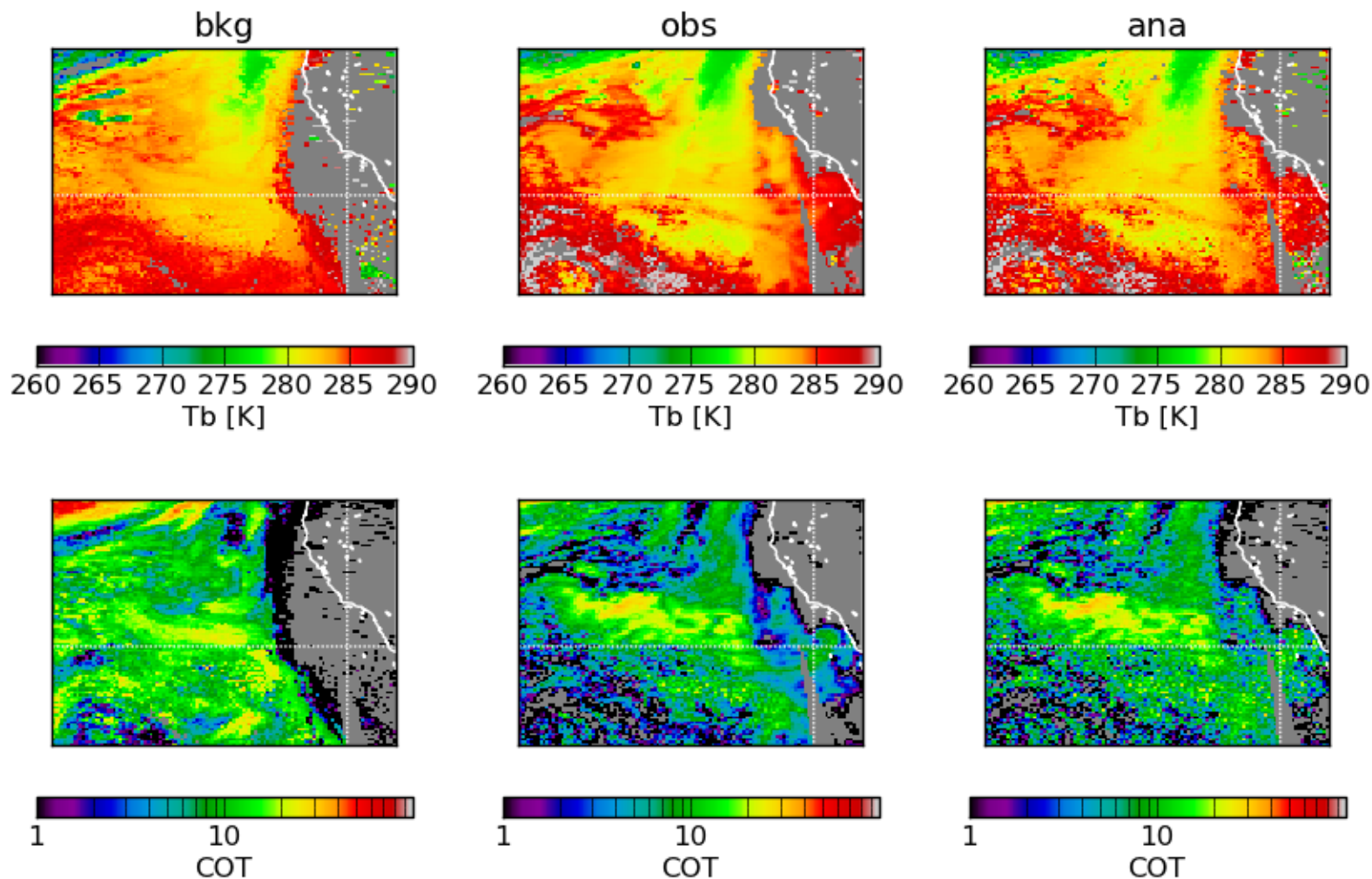
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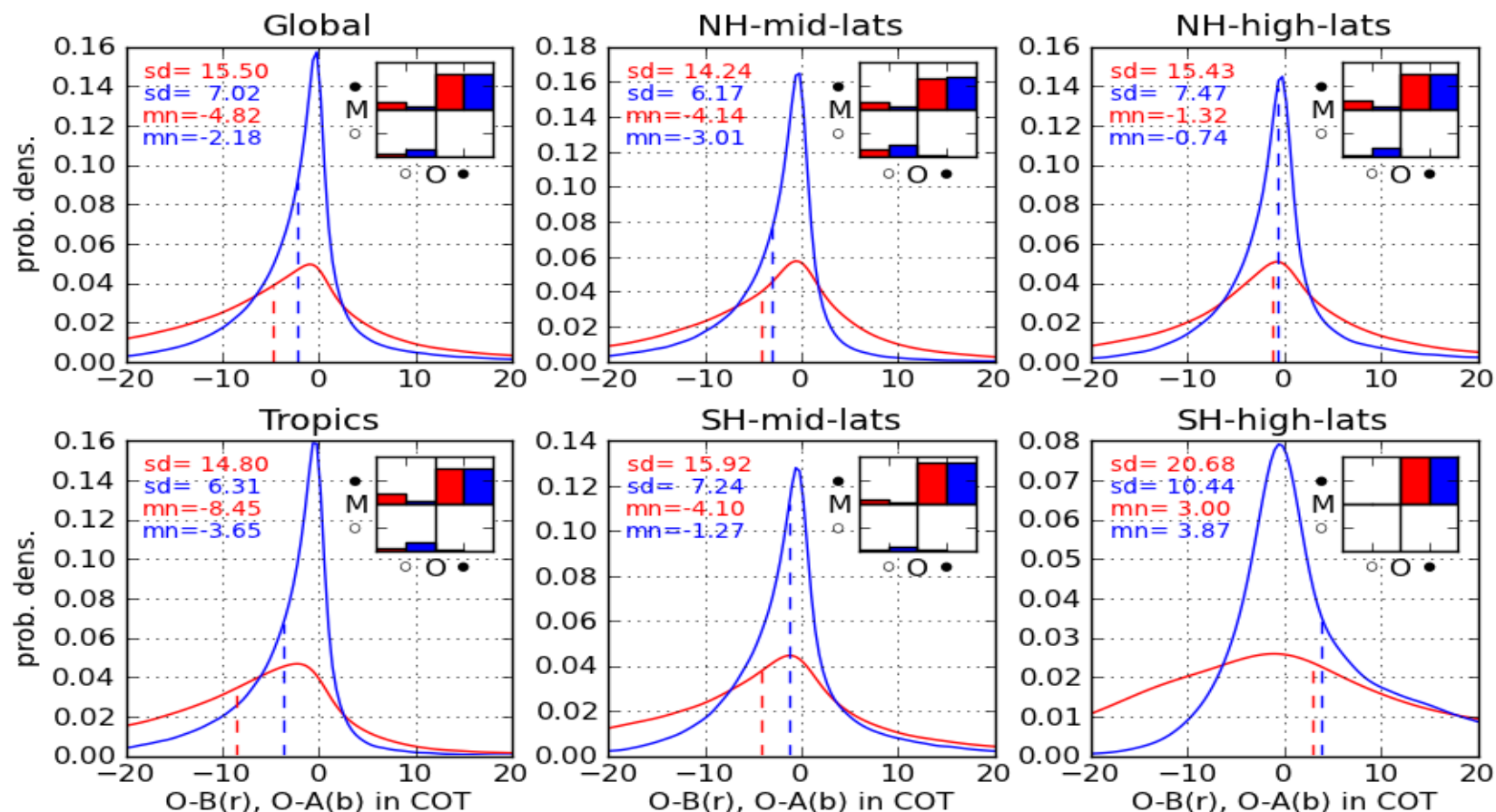


# Californian Stratocumulus



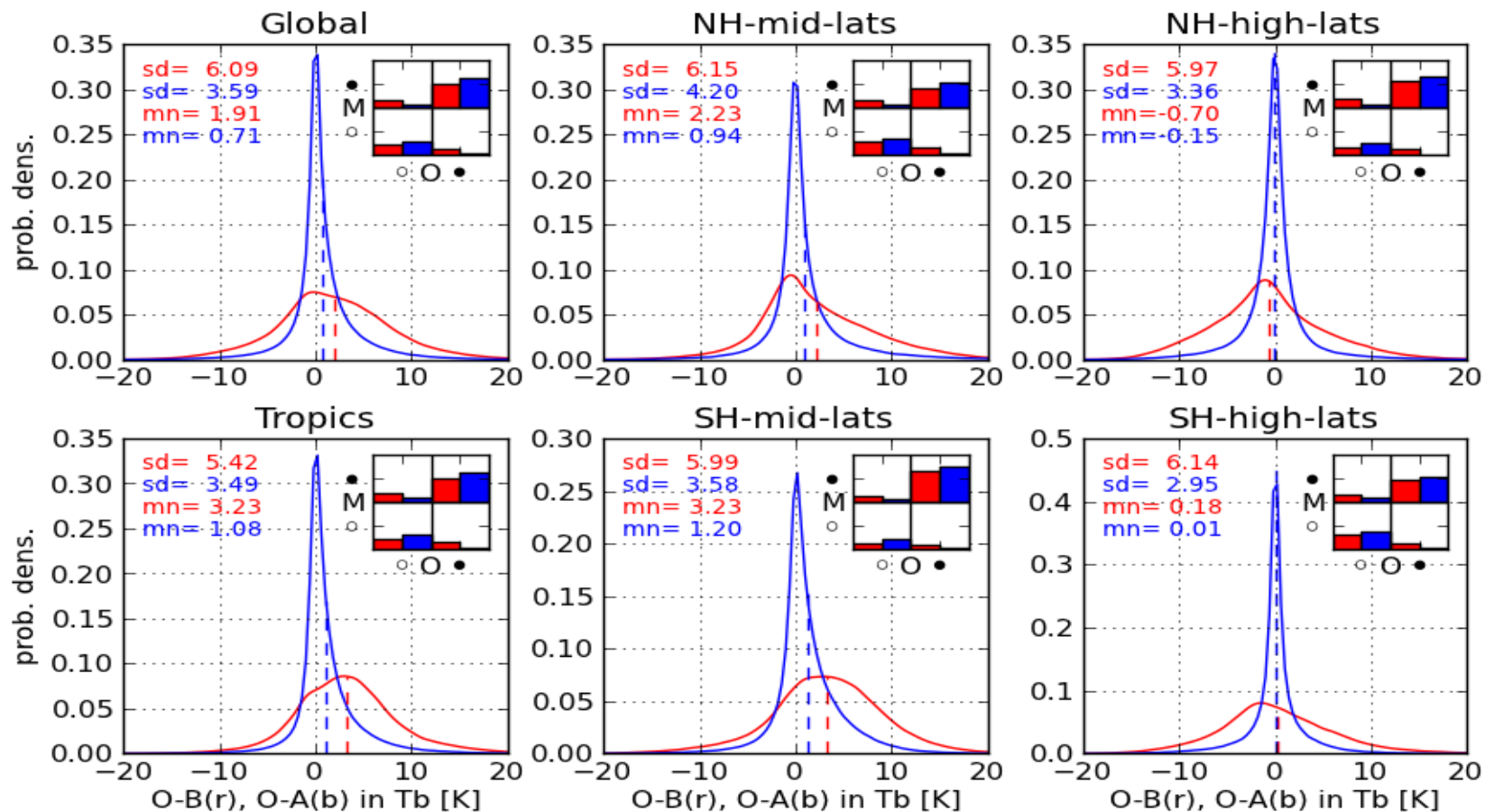


# Grid-mean Cloud Optical Depth



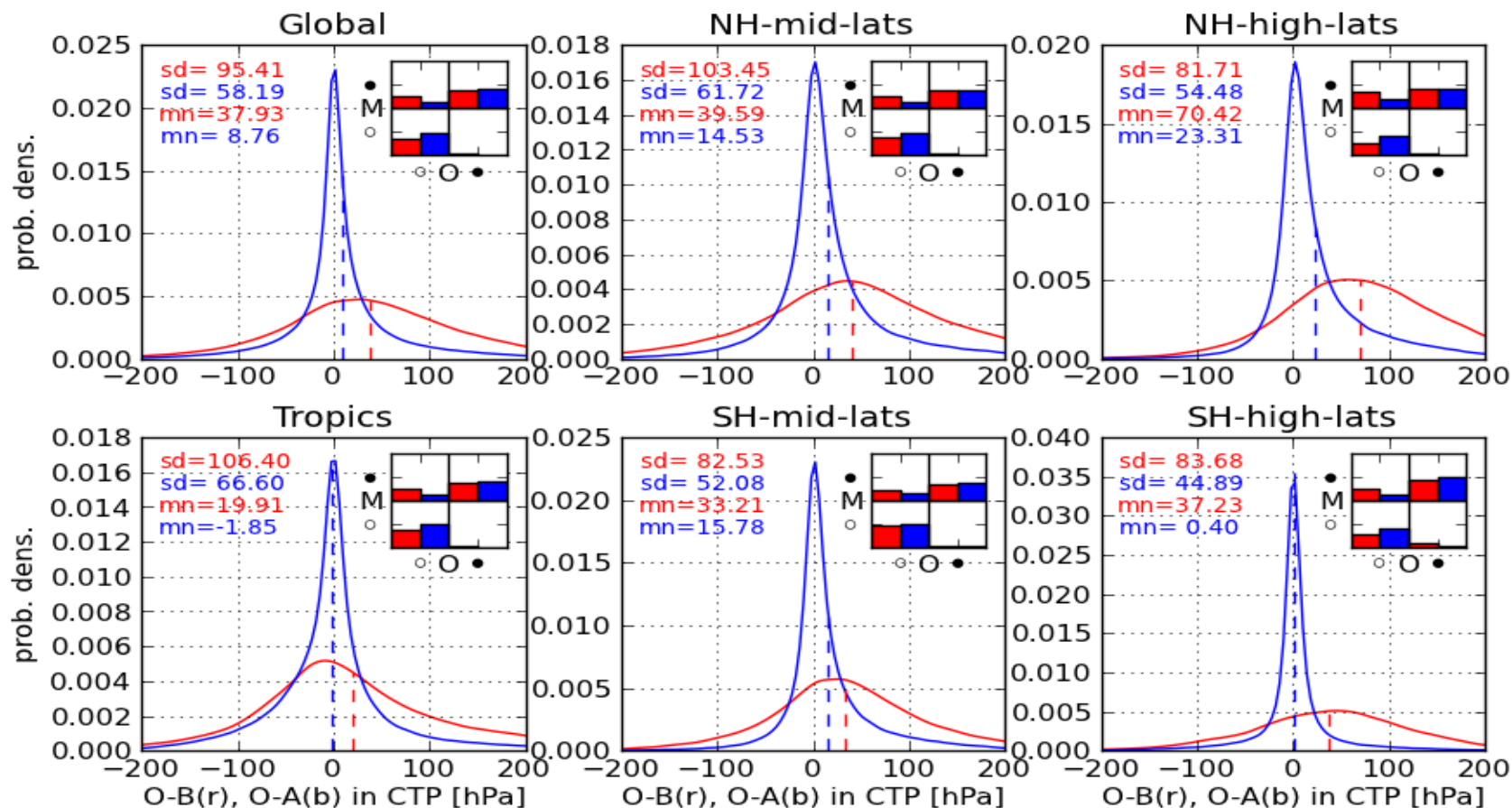
Background, Analysis

# Brightness temperature



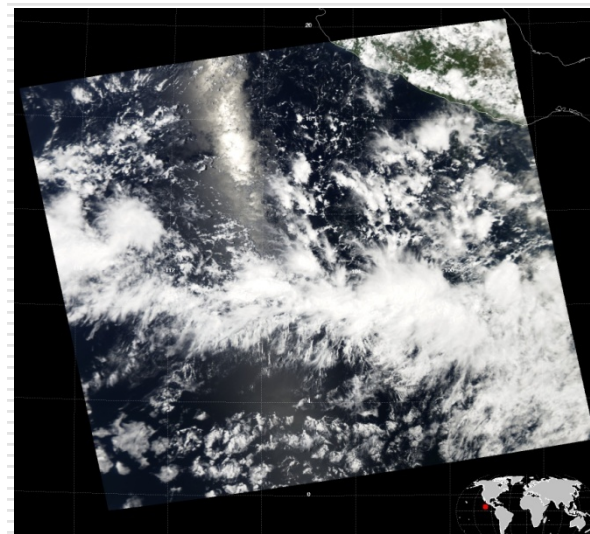
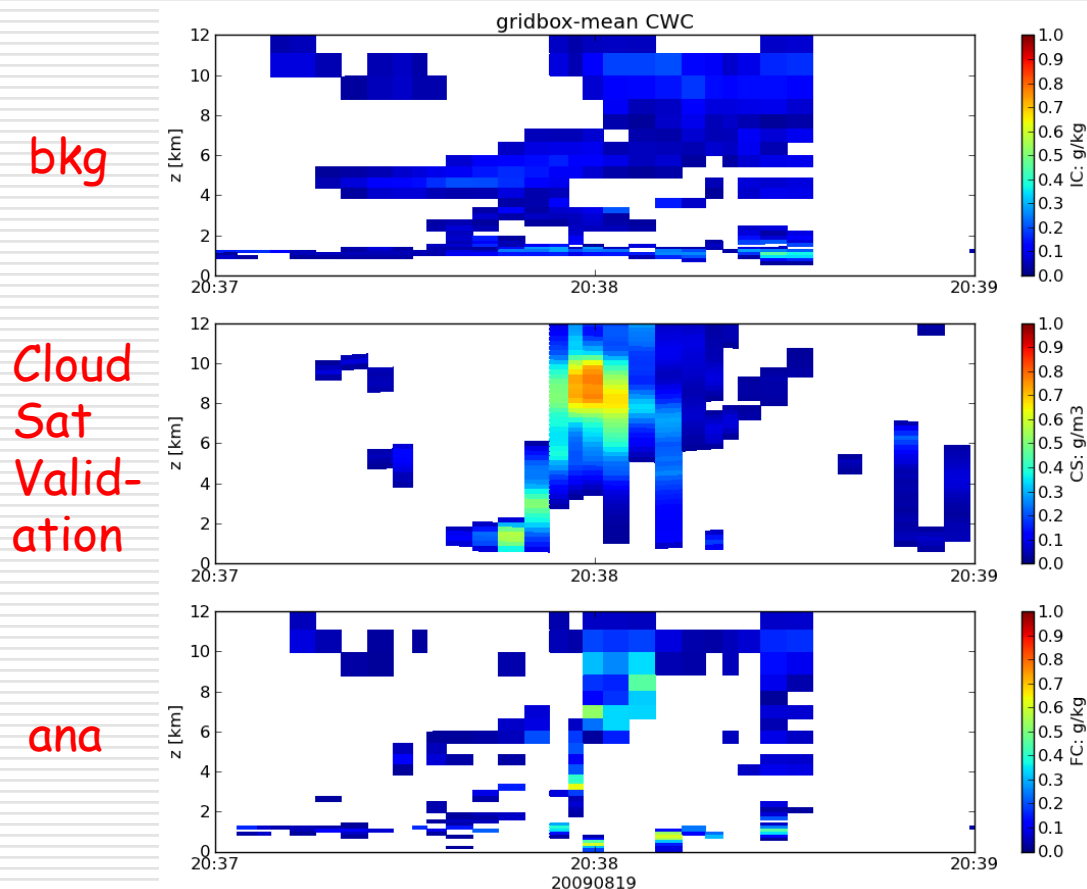
Background, Analysis  
(lower clouds,  $p > 550$  hPa)

# Cloud-Top Pressure



Background, Analysis  
(upper clouds,  $p < 550$  hPa)

# Vertical Cloud Structure -- ITCZ

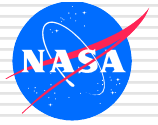




# Concluding Remarks

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- ❑ Representation of clouds in GEOS-5 is becoming good enough to warrant assimilation of cloudy data
  - ❑ High resolution MODIS/Geostationary data useful to constrain total water PDFs in GEOS-5
    - “Cloud Bias Corrector” or “Cloud Relocator”
  - ❑ Improved cloud background are essential for effective assimilation of cloudy radiances in GSI
  - ❑ Data retention requires high degree of consistency across GCM and assimilation algorithms.
  - ❑ Speed: now about 15 d/d for SEVIRI.
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# The End

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