

***Comparison of tropospheric  
humidity from AIRS, MLS, and  
theoretical Models***

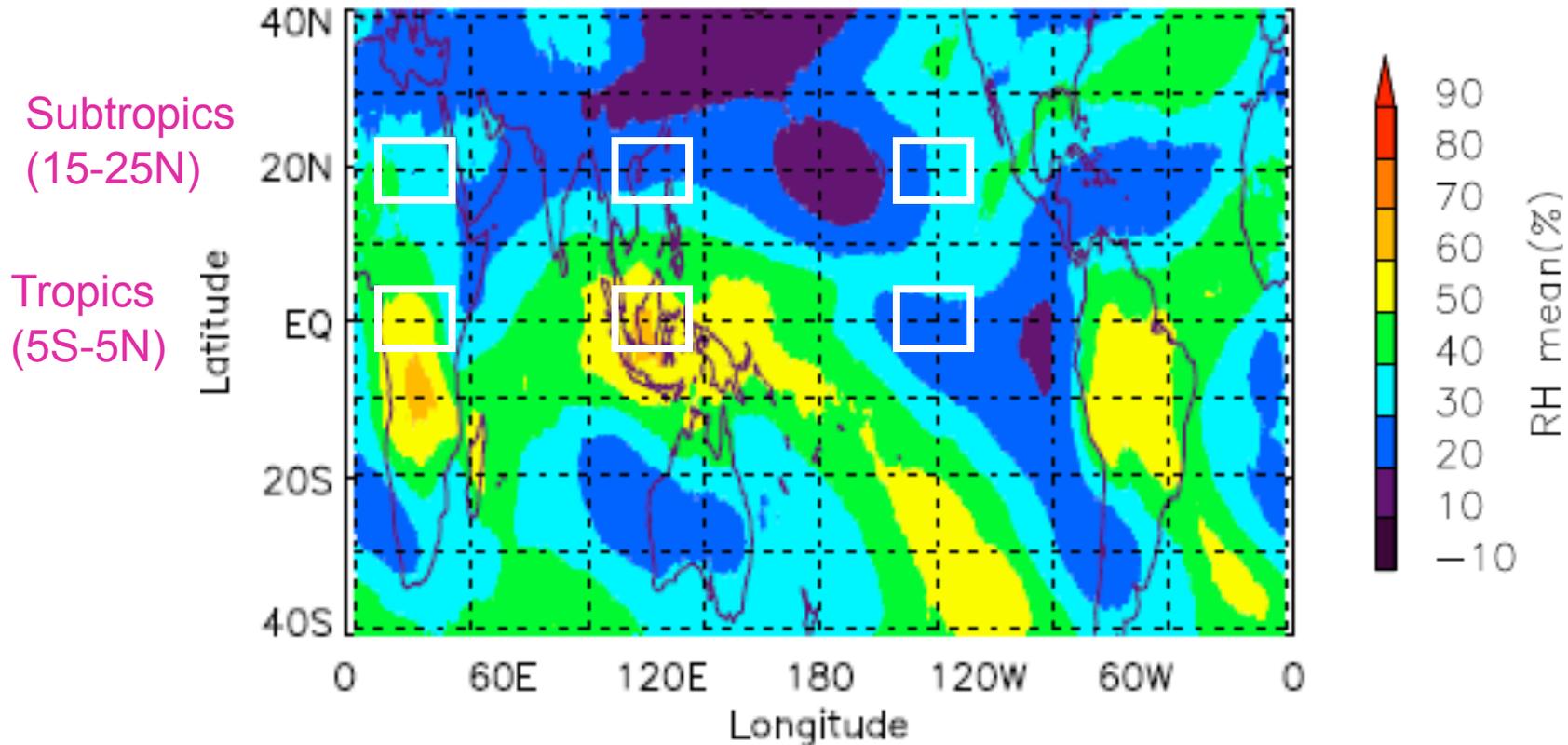
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# *Introduction*

- Climate is sensitive to upper tropospheric humidity, and it is important to know
  - *distributions* of water vapor in this region, and
  - *processes* that determine these distributions.
- We examine the **probability distribution functions (PDFs)** of upper tropospheric relative humidity (RH) for measurements from
  - Aqua AIRS
  - Aura MLS
  - UARS MLS
- Consider spatial variations of PDFs. Focus here on DJF, ~250hPa
- Also compare with **theoretical models** (generalization of Sherwood et al (2006) model).

# *Climatological UT Relative Humidity*

DJF (2002-2007) 200-250hPa  
Mean Relative Humidity (AIRS)



- Subtropics is drier than the Tropics
- But also significant zonal variations

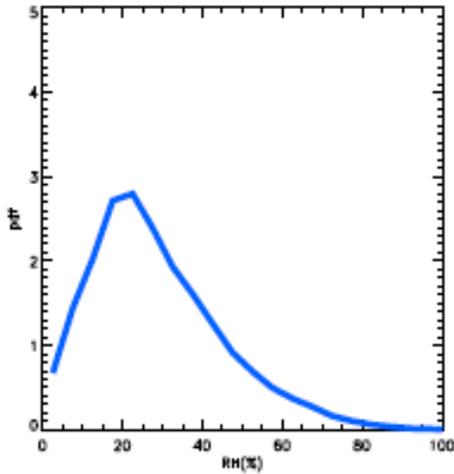
200-250hPa

# PDFs: AIRS

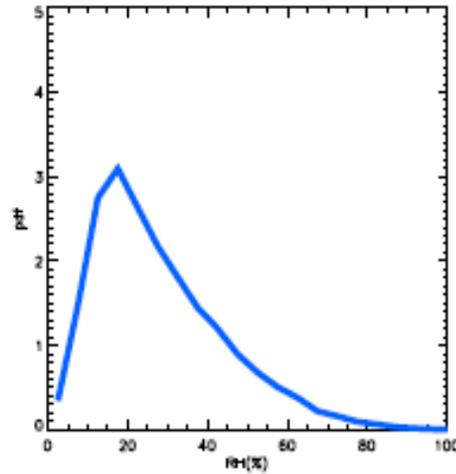
Large variation in PDFs - peak, spread, skewness, ...

Subtropics  
(15-25N)

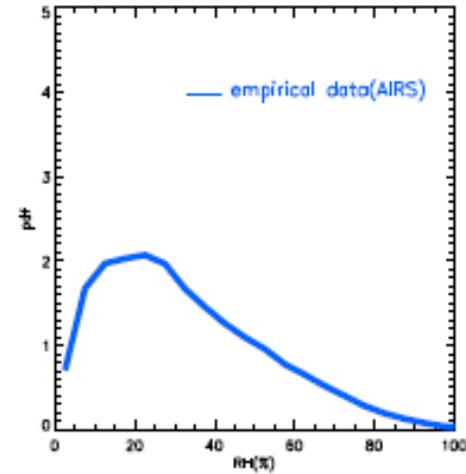
40E-60E



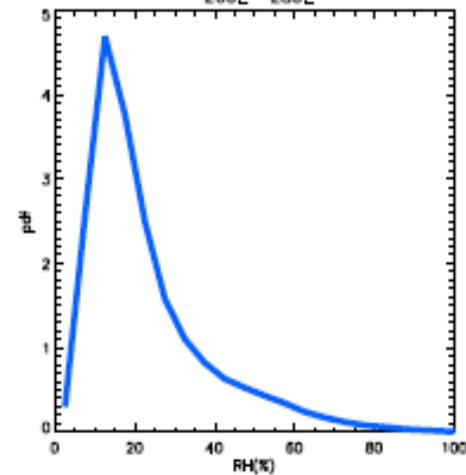
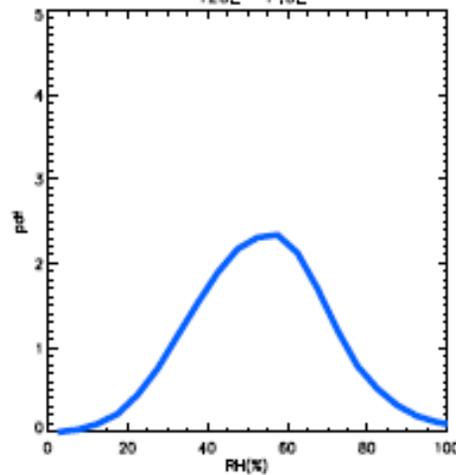
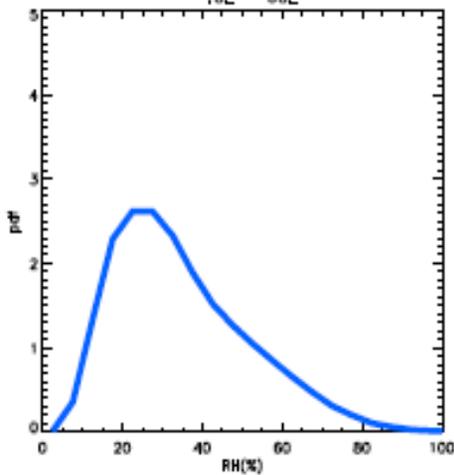
120E-140E



260E-280E



Tropics  
(5S-5N)

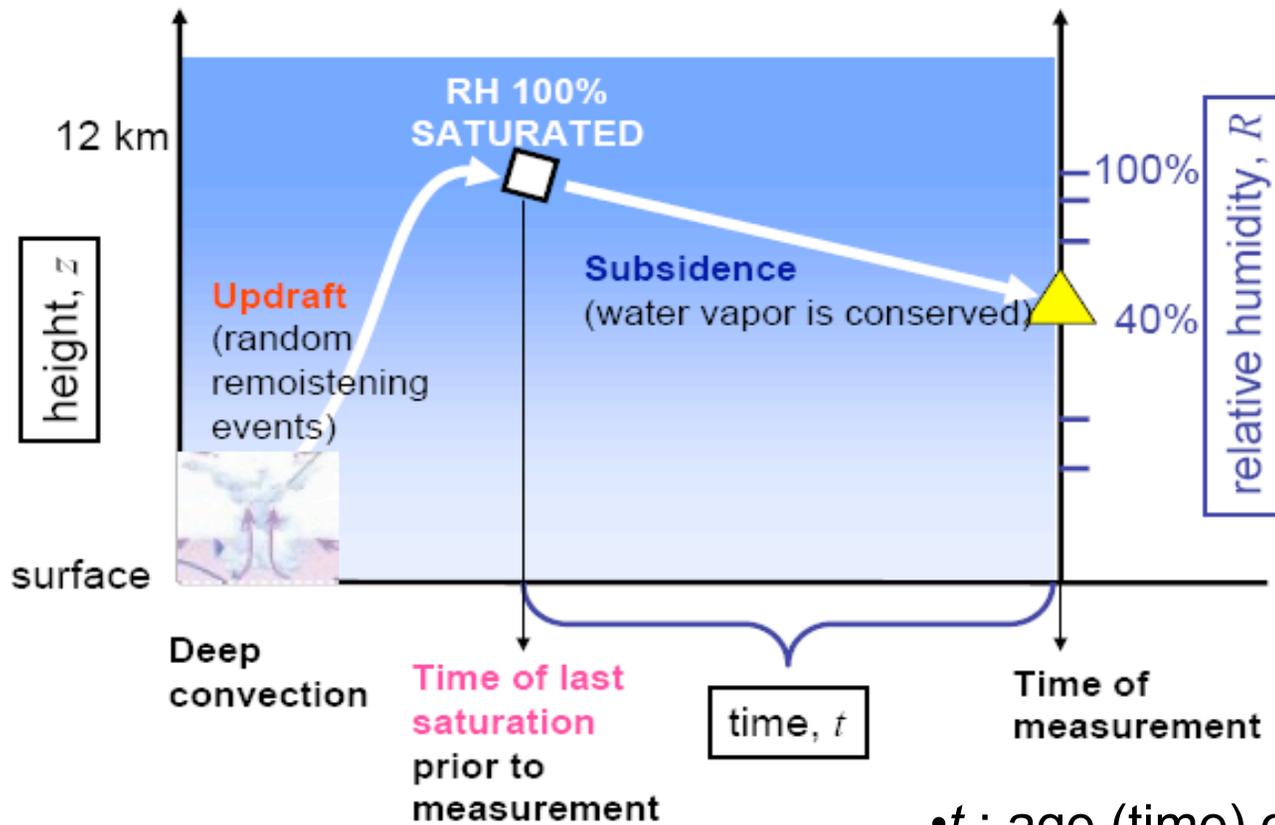


0 RH (%) 100

# Theoretical Models

## Basic Assumption:

- Moistening by random events
- Uniform Subsidence (water is conserved)



•  $t$  : age (time) of parcel since last saturation

## Theoretical Model: Generalized Version

As in the Sherwood et al. (2006) model, given uniform subsidence, RH can be approximated as

$$R(t) \approx \exp\left(-\frac{t}{\tau_{Dry}}\right)$$

Time since last saturation is now modeled as random moistening events but includes randomness of these events ( $k$ ).

$$P(t) = \frac{\left(\frac{1}{\tau_{Moist}}\right)^k \exp\left(-\frac{t}{\tau_{Moist}}\right) t^{k-1}}{\Gamma(k)}$$

Eliminate  $t$  from above equations, yields the generalized PDFs of RH as

$$P(R) = \frac{k^k r^k R^{kr-1}}{\Gamma(k)} (-\log R)^{k-1}$$

When  $k=1$  it is the same as Sherwood et al. (2006)

$$P(R) = r R^{r-1}$$

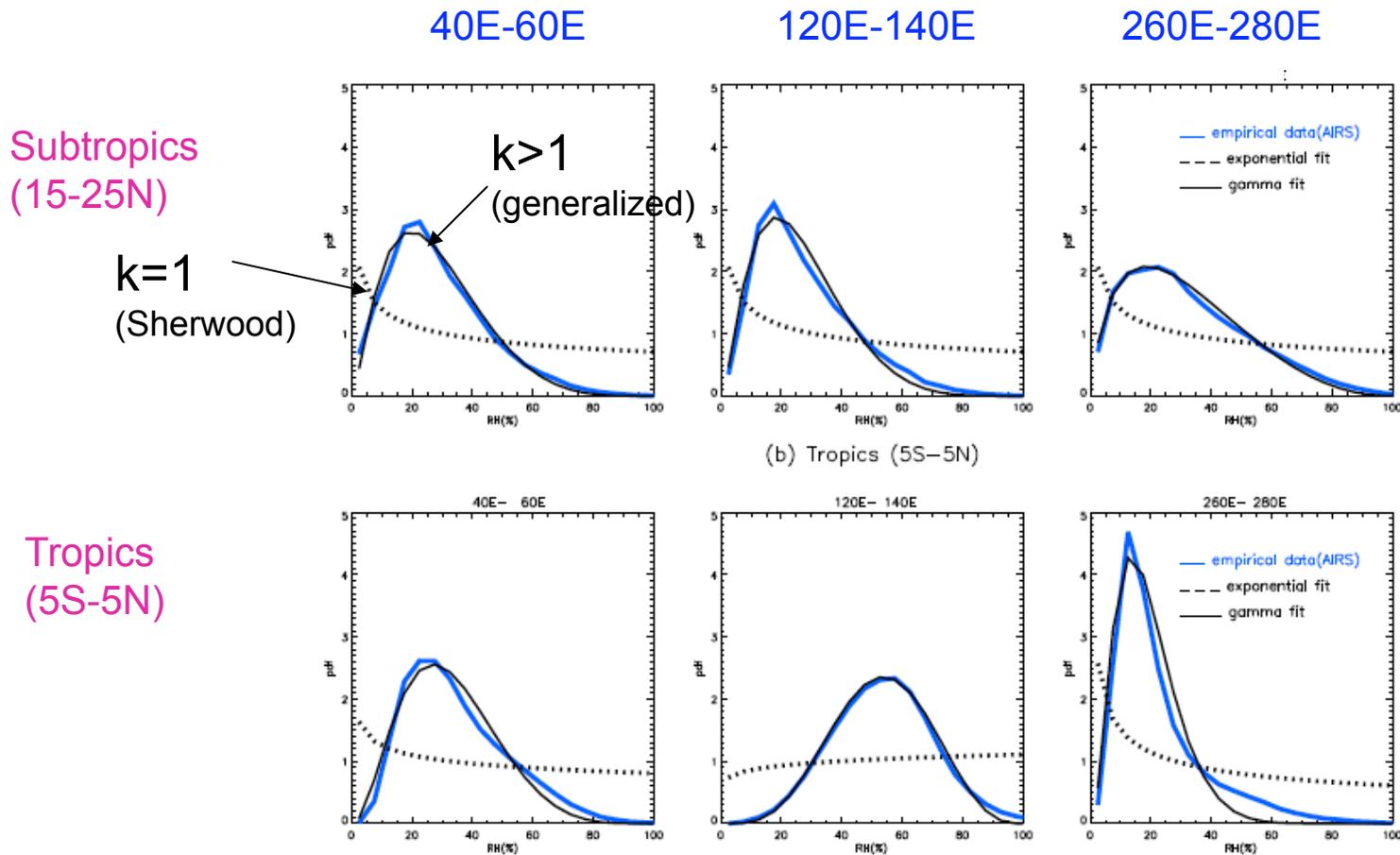
where,  $\Gamma(k)$  : Gamma function

$r$ : ratio of drying time ( $\tau_{dry}$ ) to moistening time ( $\tau_{moist}$ )

$k$ : measure of randomness of remoistening events

# PDFs: Data and Model

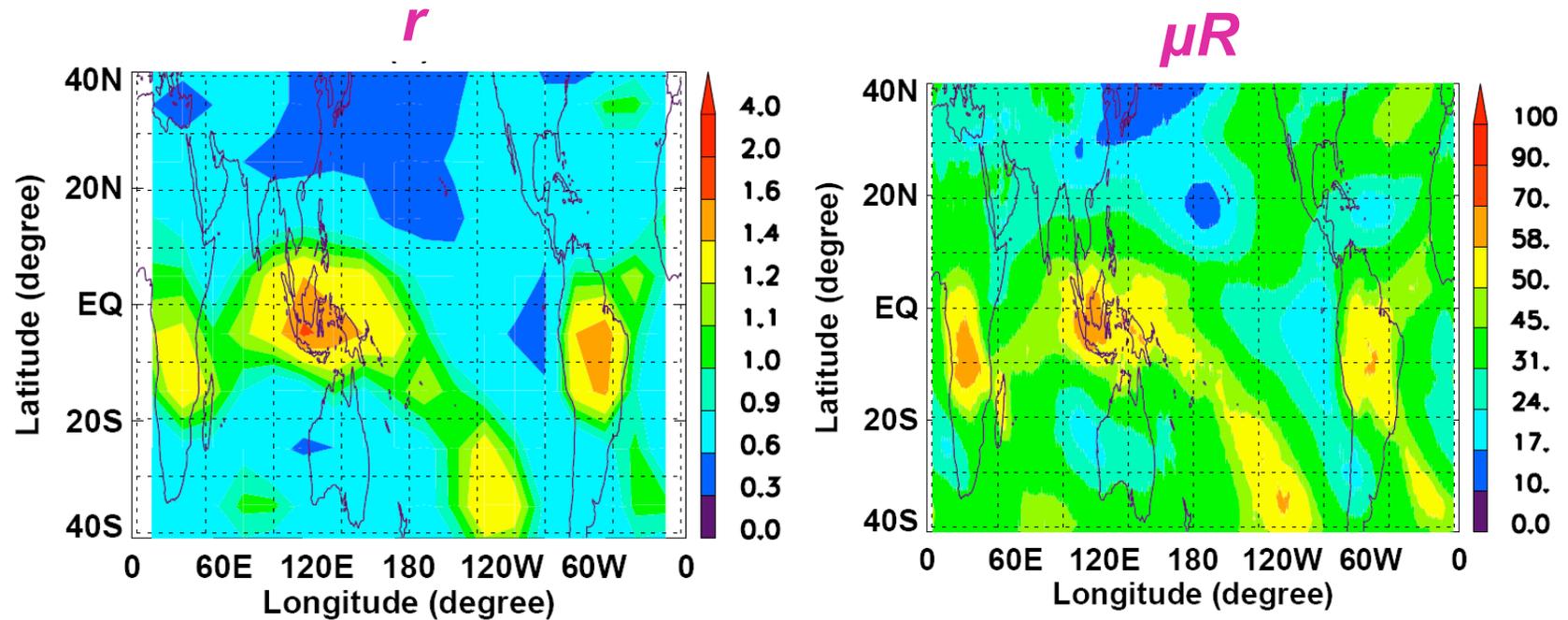
How well do the theoretical models fit the observed PDFs?



Generalized Model can fit the observed PDFs (peak, spread, skewness), with  $r$  and  $k$  varying with location.

# Maps of “ $r$ ” and “mean RH”

AIRS (2002-2007)

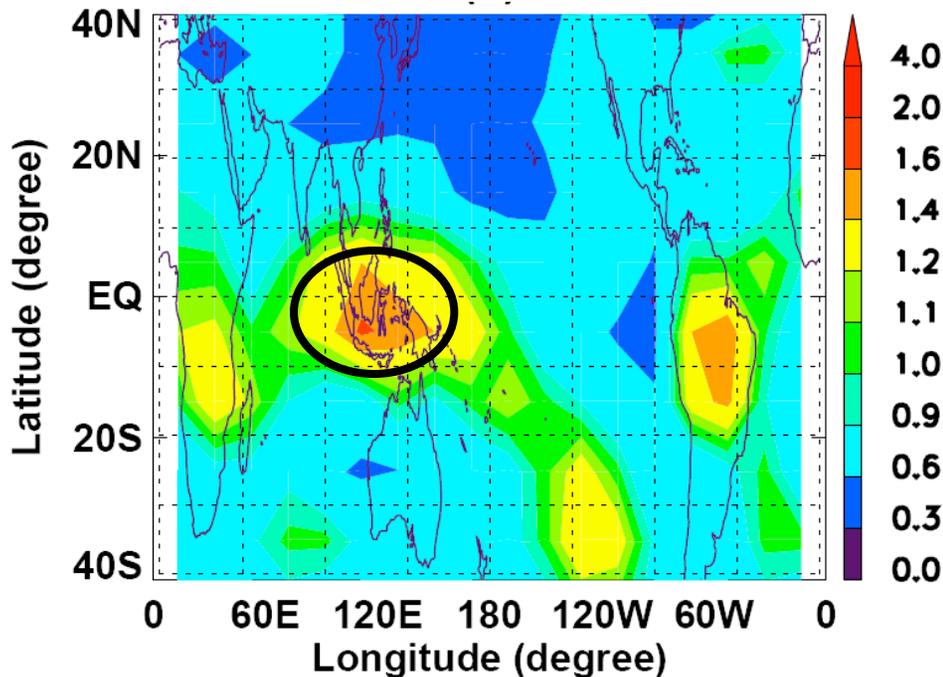


**Strong resemblance** between maps of  $r$  and **mean RH ( $\mu R$ )**

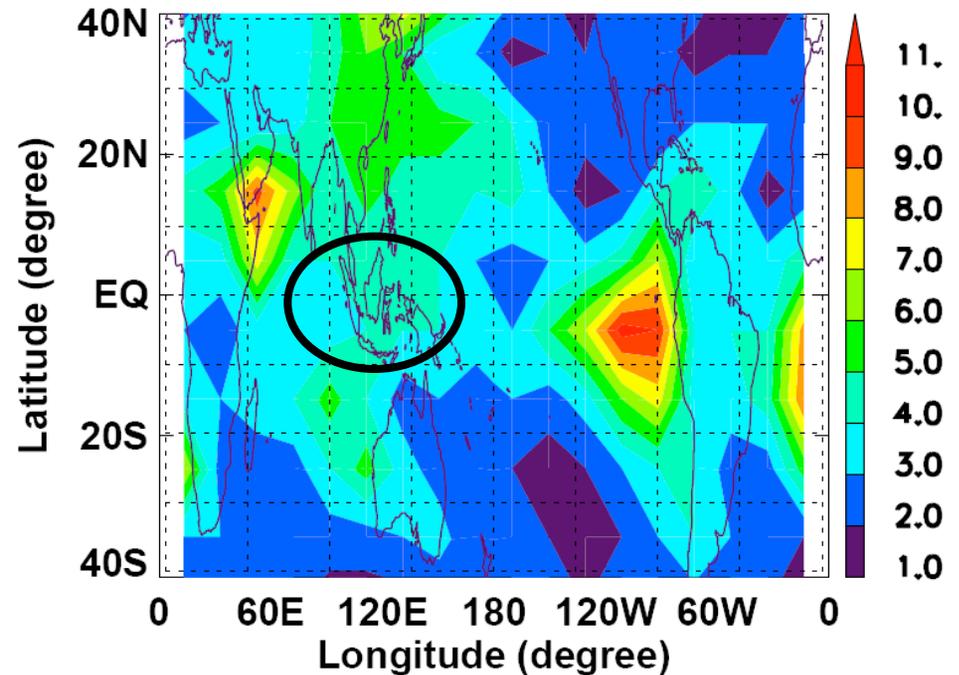
# Maps of “ $r$ ” and “ $k$ ”

AIRS (2002-2007)

$r$



$k$



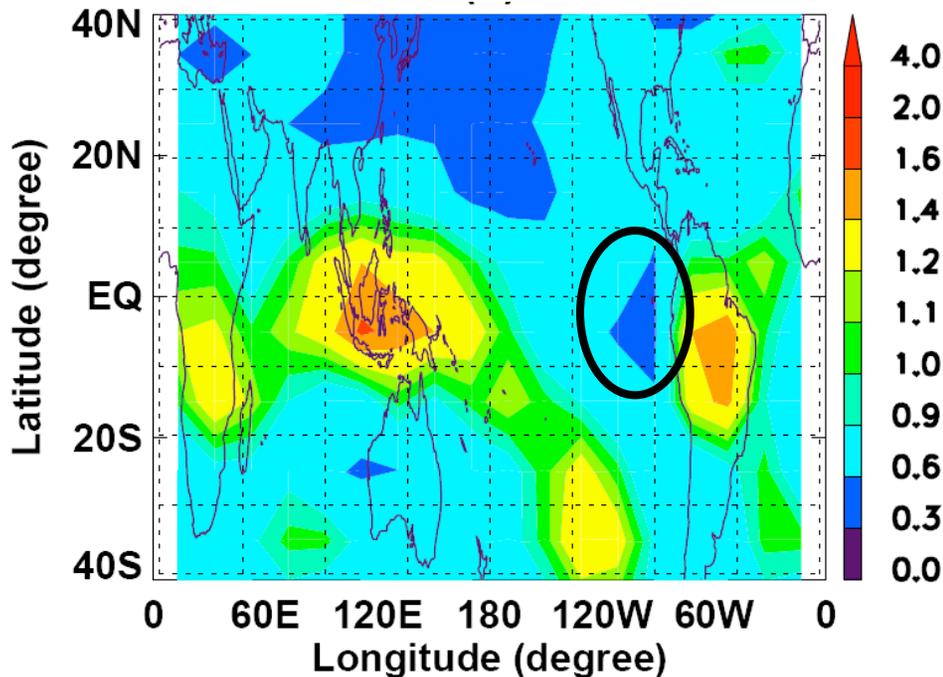
## Convective Regions:

- large  $r$  ( $r > 1$ ) and small  $k$   
=> Rapid, random remoistening

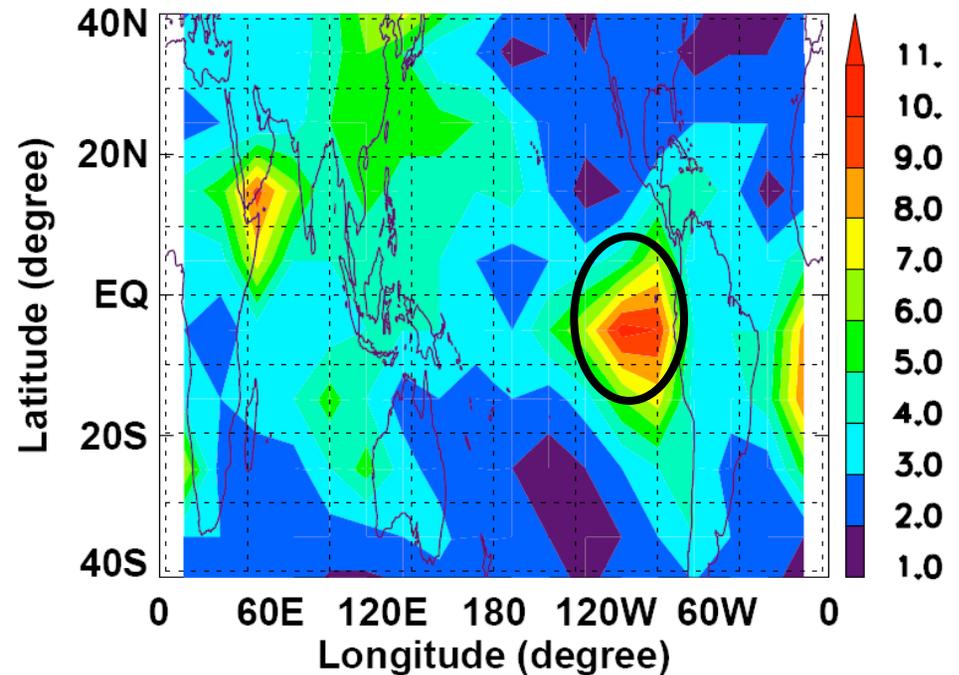
# Maps of “ $r$ ” and “ $k$ ”

AIRS (2002-2007)

$r$



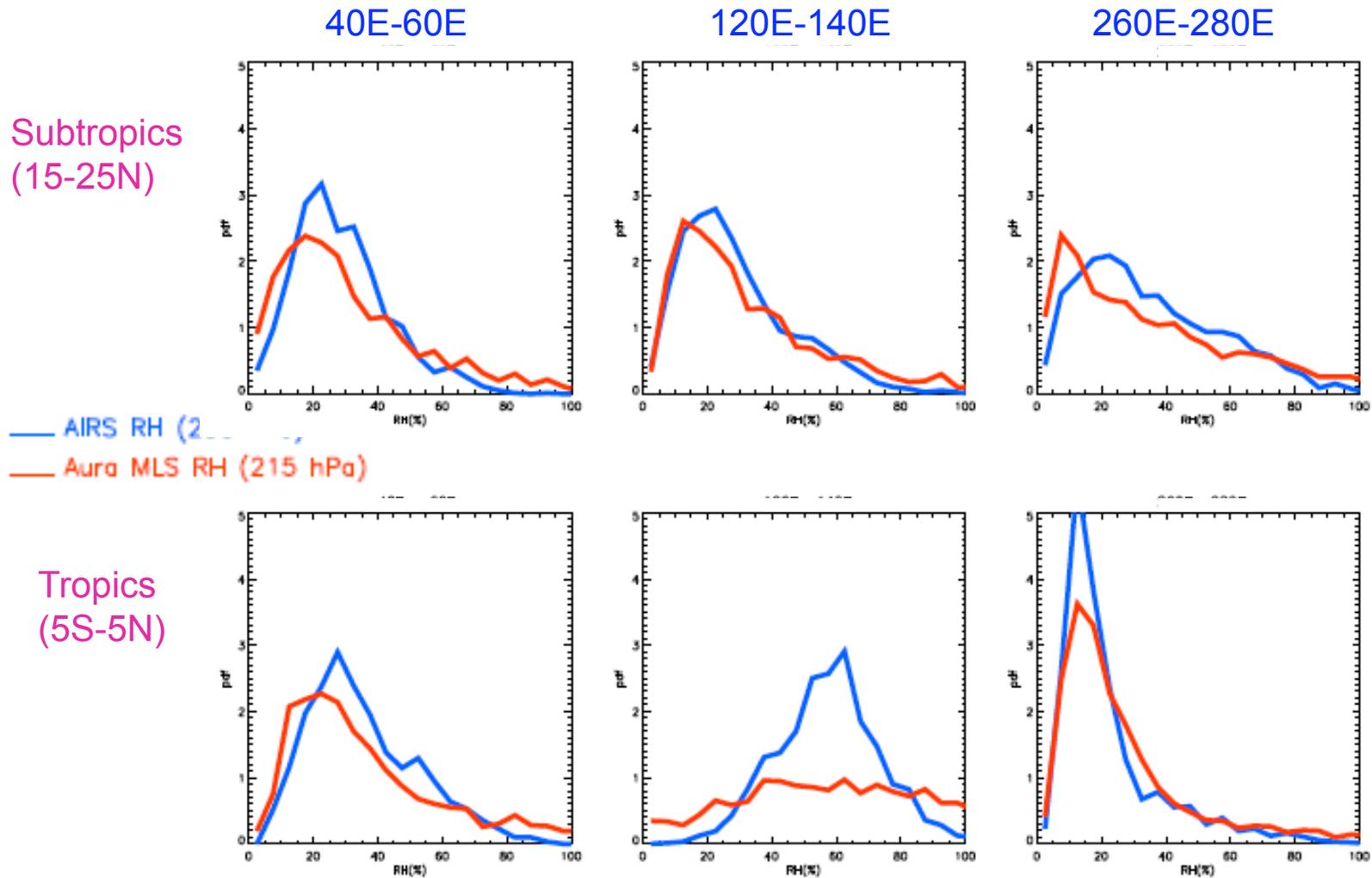
$k$



## Non-convective Regions:

- **small  $r$  ( $r < 1$ ) and large  $k$**   
=> Slower, more regular  
remoistening (horizontal transport)

# PDFS: AIRS - Aura MLS Comparison

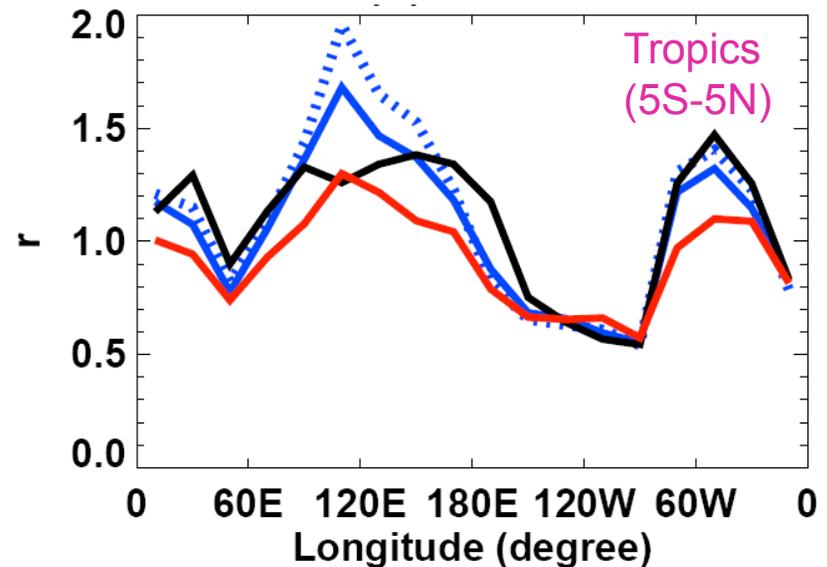
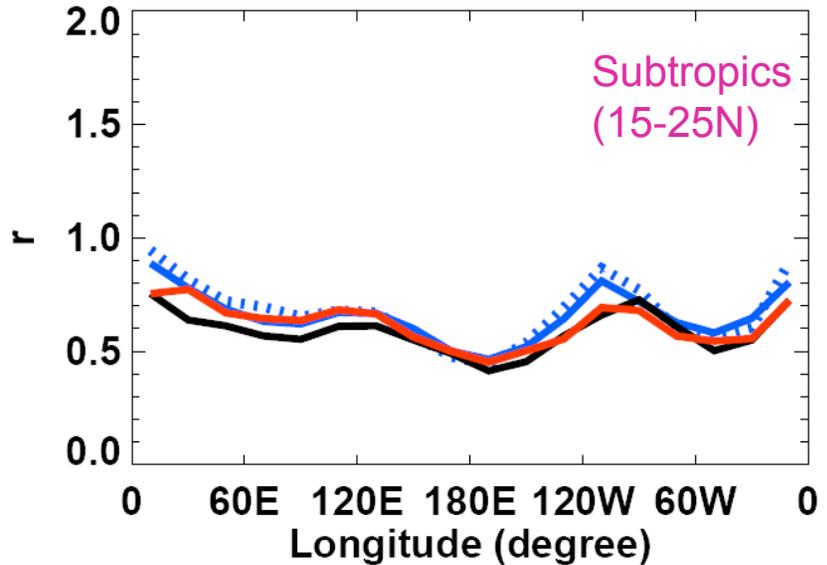
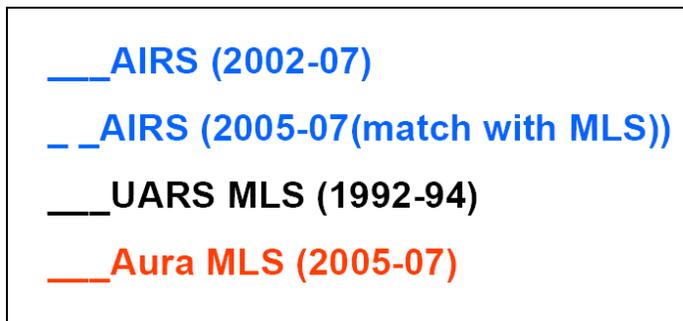


Good agreement between AIRS and Aura MLS,  
with some exceptions.

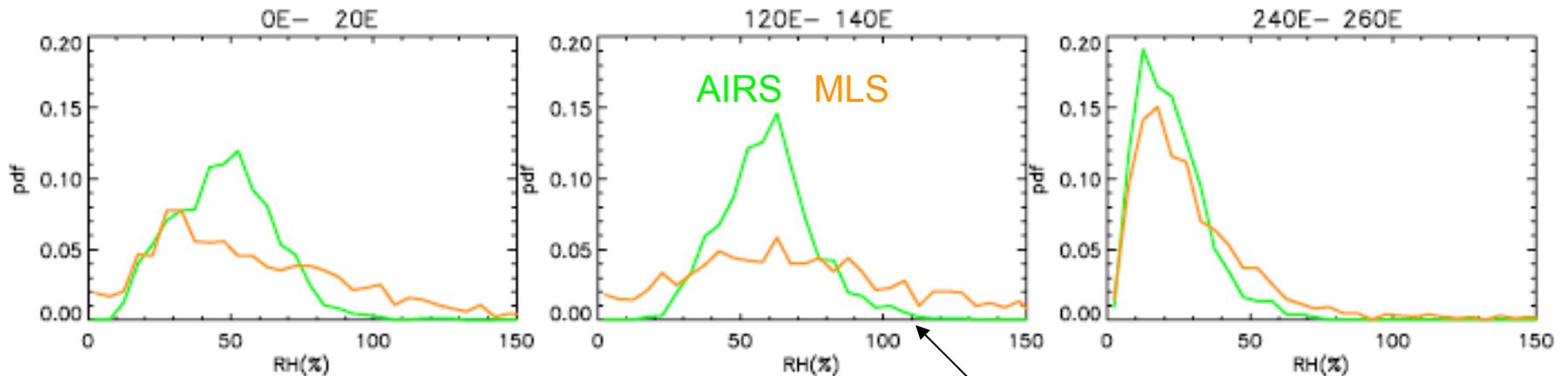
# Spatial Variations in $r$

$$r = \tau_{\text{dry}} / \tau_{\text{moist}}$$

- Good agreement between different data sets.
- All show
  - $r > 1$  in tropical convective regions,
  - $r < 1$  in dry regions.
- Expected as larger  $r$  implies more rapid remoistening



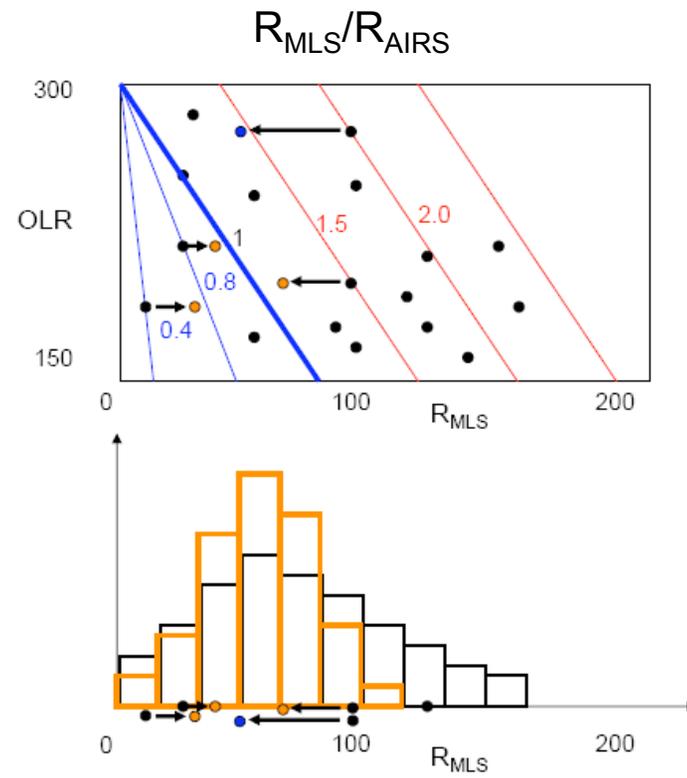
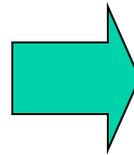
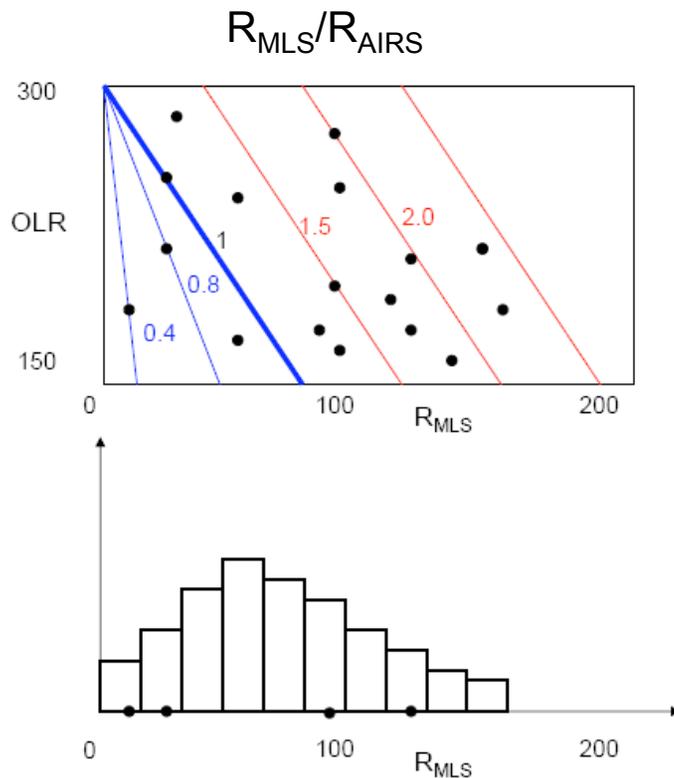
## AIRS - Aura MLS bias



**Largest difference: Tropical convective regions (5S-5N, 120-140E)**

- There are some differences between AIRS and MLS PDFs.
- Differences are not simply a function of RH.
- Is there a simple parameterization of the AIRS-MLS difference?

# Bias between data: $R_{MLS}/R_{AIRS}$

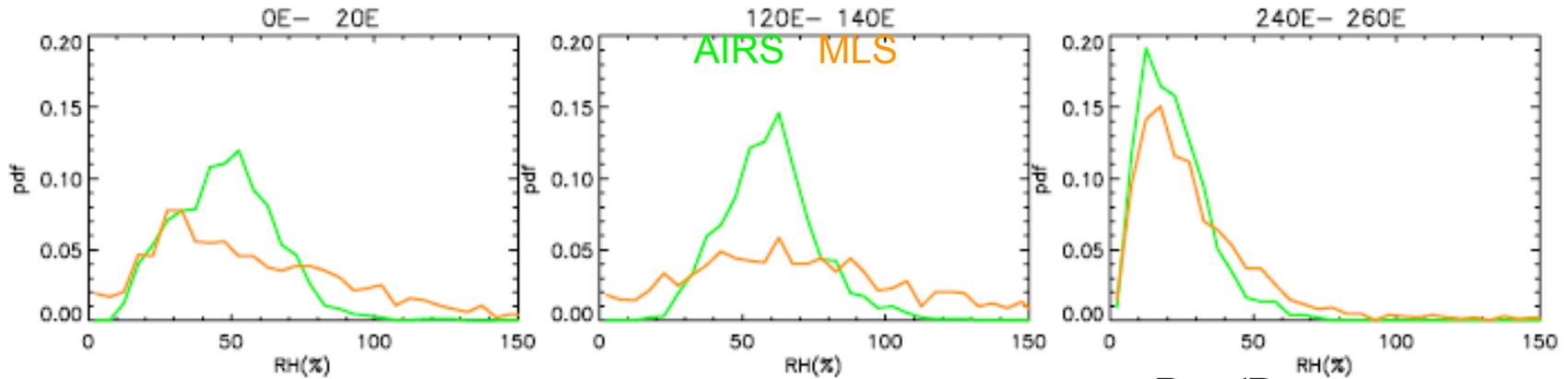


NOAA spatially and temporally interpolated OLR (2005-2006)

**PDFs of MLS data**

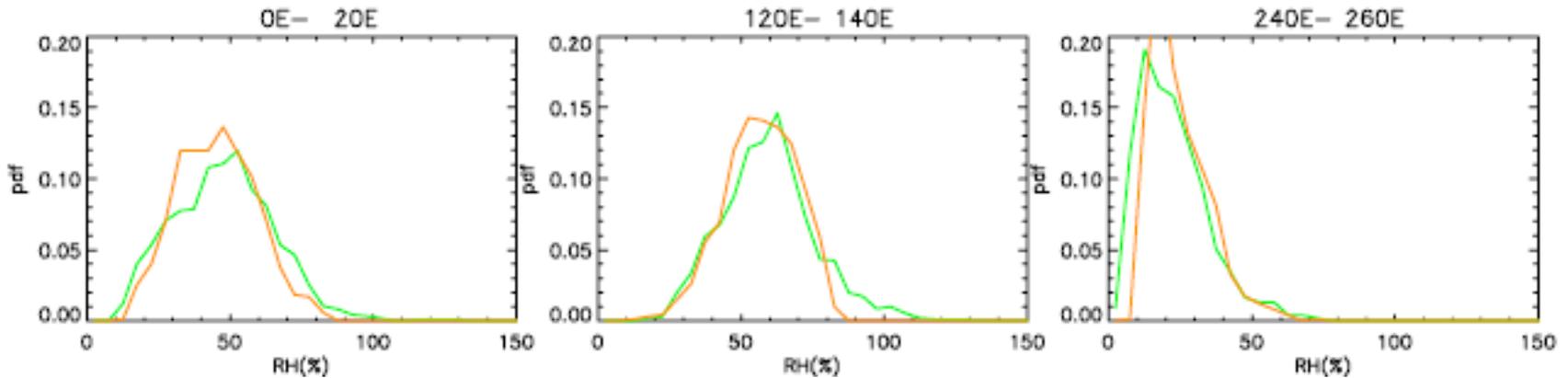
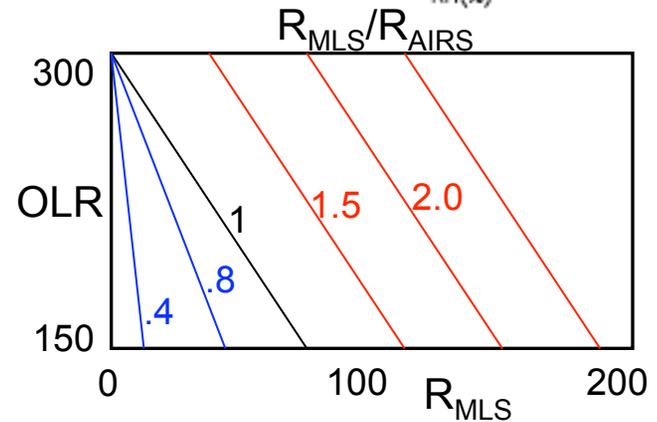
**PDFs of MLS data *after transform***

# AIRS - Aura MLS bias



Transform  
MLS Data

$$R_{\text{MLS}}/R_{\text{AIRS}} = f(R_{\text{MLS}}, \text{OLR})$$



# Conclusions

- Several robust features (peak, range, skewness) are found in the observed PDFs from all three data-sets (Aura and UARS MLS, AIRS).
- All can be well fit by a generalized version of the Sherwood et al. (2006) theoretical model.
- Consistent spatial variations in “ $r$ ” (ratio of drying and moistening times) and “ $k$ ” (randomness of moistening process).

- Large  $r$ , small  $k$  in tropical convective regions  
→ rapid, random remoistening
- Small  $r$ , large  $k$  in dry regions  
→ slow, more regular remoistening

- A more quantitative link between the different physical processes and the parameters  $r$  and  $k$  is needed. This would be performed by trajectory-based water vapor simulations.

## Theoretical Model: Sherwood et al (2006)

Sherwood et al. (2006) assumed that if parcels uniformly subside, RH can be approximated as

$$R(t) \approx \exp\left(-\frac{t}{\tau_{Dry}}\right)$$

Time since last saturation is modeled as time between random moistening events

$$P(t) = \exp(-t/\tau_{moist})/\tau_{moist}$$

Eliminate  $t$  from above equations, yields the PDFs of RH as

$$P(R) = r R^{r-1}$$

where,

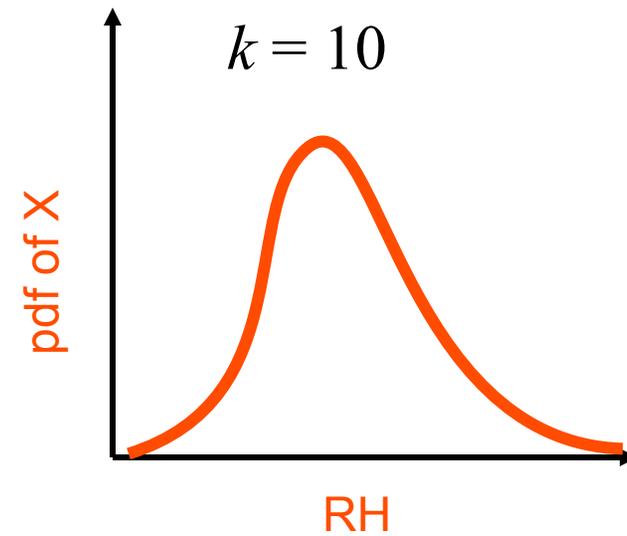
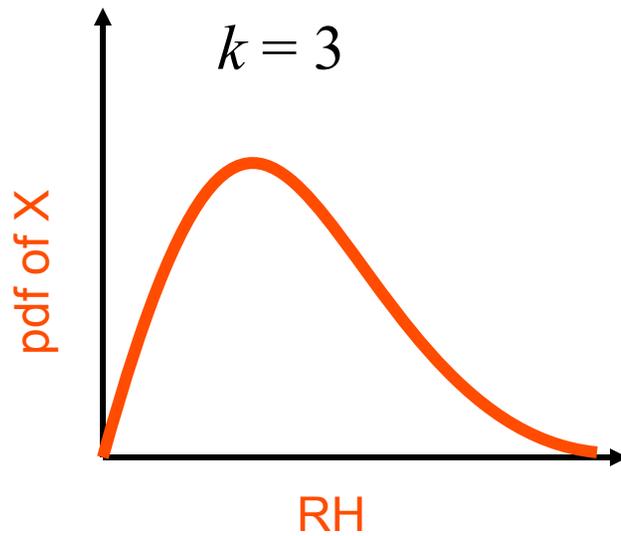
$$r = \tau_{dry}/\tau_{moist}$$

$\tau_{dry}$  is the uniform drying time by subsidence  
 $\tau_{moist}$  is the time between remoistening events.

# Characteristics of the Gamma PDF

$k = 1$  Gamma PDF = Exponential PDF

$$k > 1 \quad k \propto \left( \frac{\text{mean(RH)}}{\text{standard deviation(RH)}} \right)^2$$



$k$  : randomness parameter

Large  $k \Rightarrow$  less random moistening events

- Variations in  $r$  and  $k$  characterize variations in the moistening processes.
- The maps of  $\mu_R$  and  $\sigma_R$  show a strong resemblance to those of  $r$  and  $k$ , respectively, i.e., there is **large**  $\mu_R$  where  $r$  is **large** and **large**  $\sigma_R$  where  $k$  is **small**.

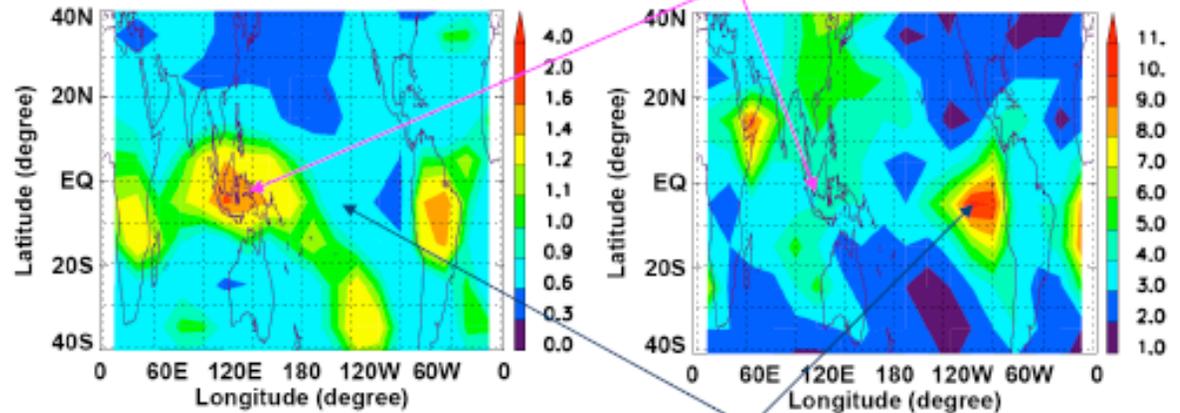
$$r \sim \mu_R$$

$$k \sim 1/(\sigma_R)^2$$

### Generalized model parameters

### Convective Region

**Large  $r$ :** rapid remoistening  
**Small  $k$ :** more randomness



### AIRS RH 250 hPa

### Non-convective Region

**Small  $r$ :** slow remoistening  
**Large  $k$ :** less randomness

